

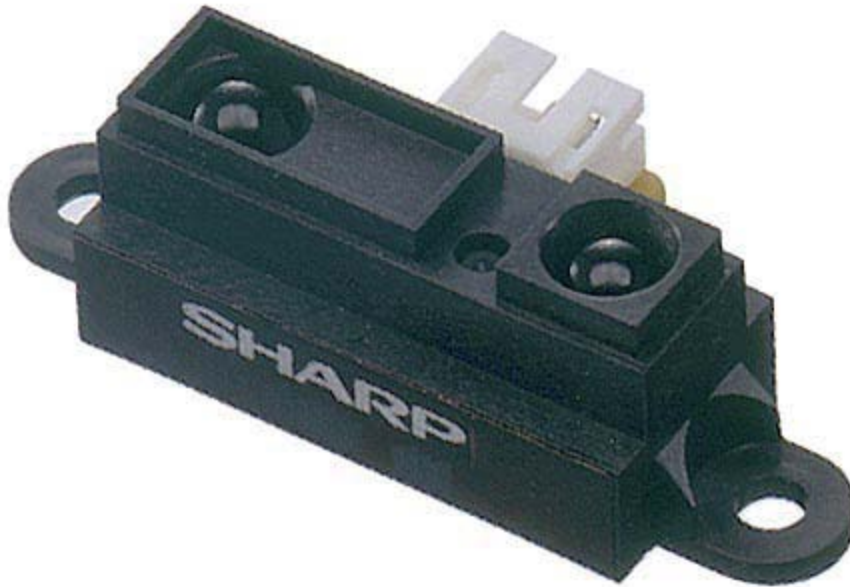
Distance Sensor Models

Range Sensors

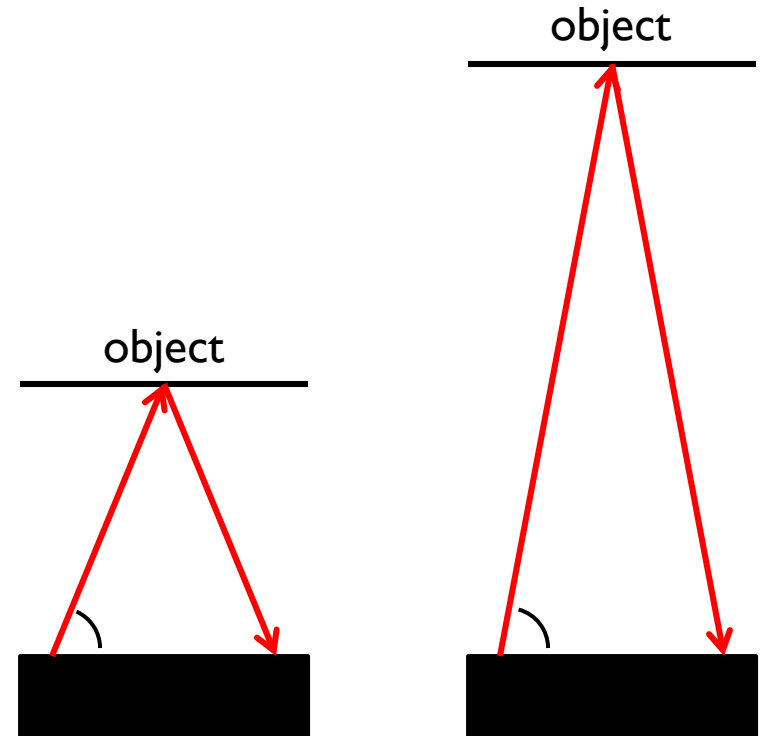
- ▶ range sensors measure the distance between the robot and the sensed object(s)
 - ▶ bearing measurement can be obtained by rotating the sensor or using multiple sensors arranged on a circular arc
- ▶ many non-vision based sensors can be modeled by measuring the distance along a beam or cone

Infra-red Range Sensor

- ▶ uses an IR LED and a linear CCD array to triangulate distances



Sharp GP2Y0A21YK0F data sheet



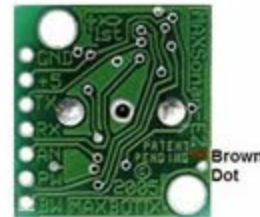
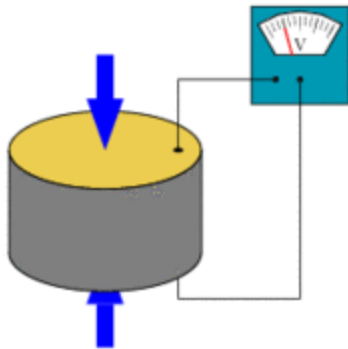
angle increases as distance increases

Infra-red Range Sensor

- ▶ has a minimum and maximum distance
 - ▶ changes depending on the model but range is on the order of a few centimeters to a few meters
- ▶ inexpensive (less than \$20)
- ▶ measurements affected by the material properties of the object
 - ▶ but less sensitive to the orientation of the reflecting surface
- ▶ low accuracy

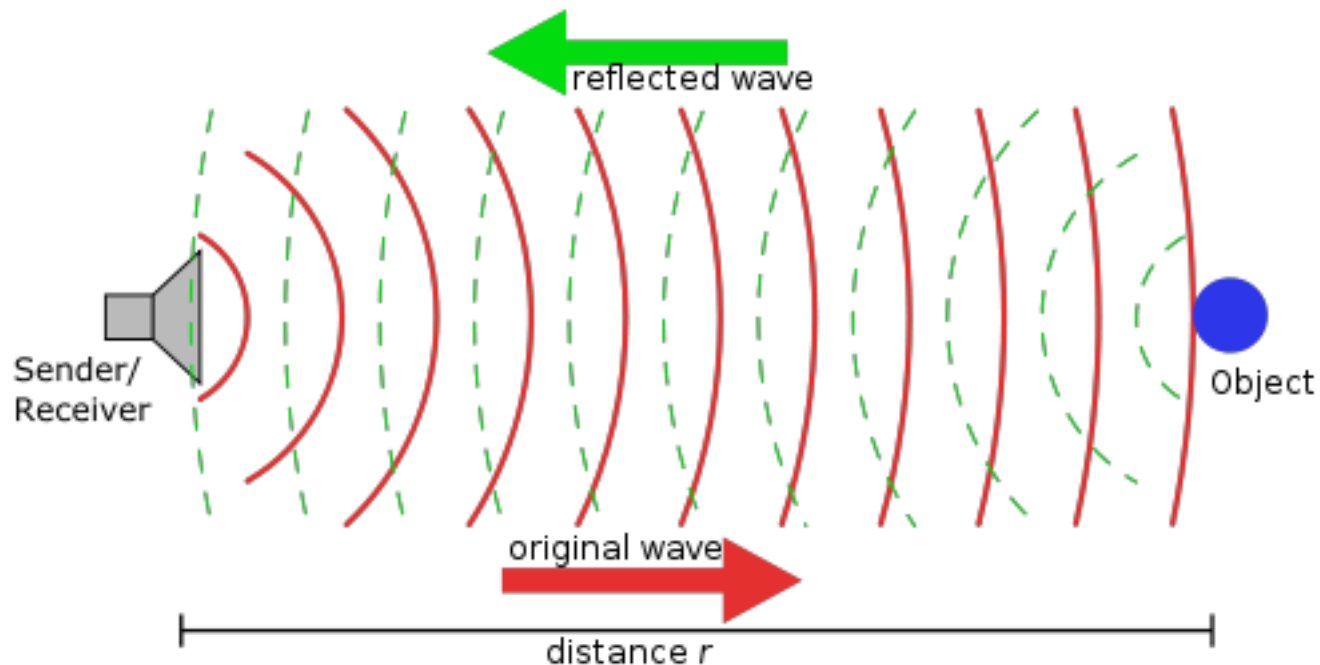
Ultrasound Range Sensors

- ▶ ultrasound is sound above the upper limit of human hearing (approximately 20,000 Hz)
- ▶ inexpensive ultrasonic transducers are essentially ceramic discs that vibrate at ultrasonic frequencies
- ▶ operate via the piezoelectric effect
 - ▶ an applied external electric field causes a small change in the physical dimensions
 - ▶ conversely, an applied stress will induce a small electric field



Ultrasound Range Sensors

- ▶ basic idea of operation is simple
 - ▶ transducer emits a short pulse of ultrasound
 - ▶ receiver listens for echo
 - ▶ time elapsed between pulse and echo is proportional to twice the distance to the object



Ultrasound Range Sensors

- ▶ speed of sound in air is given approximately by

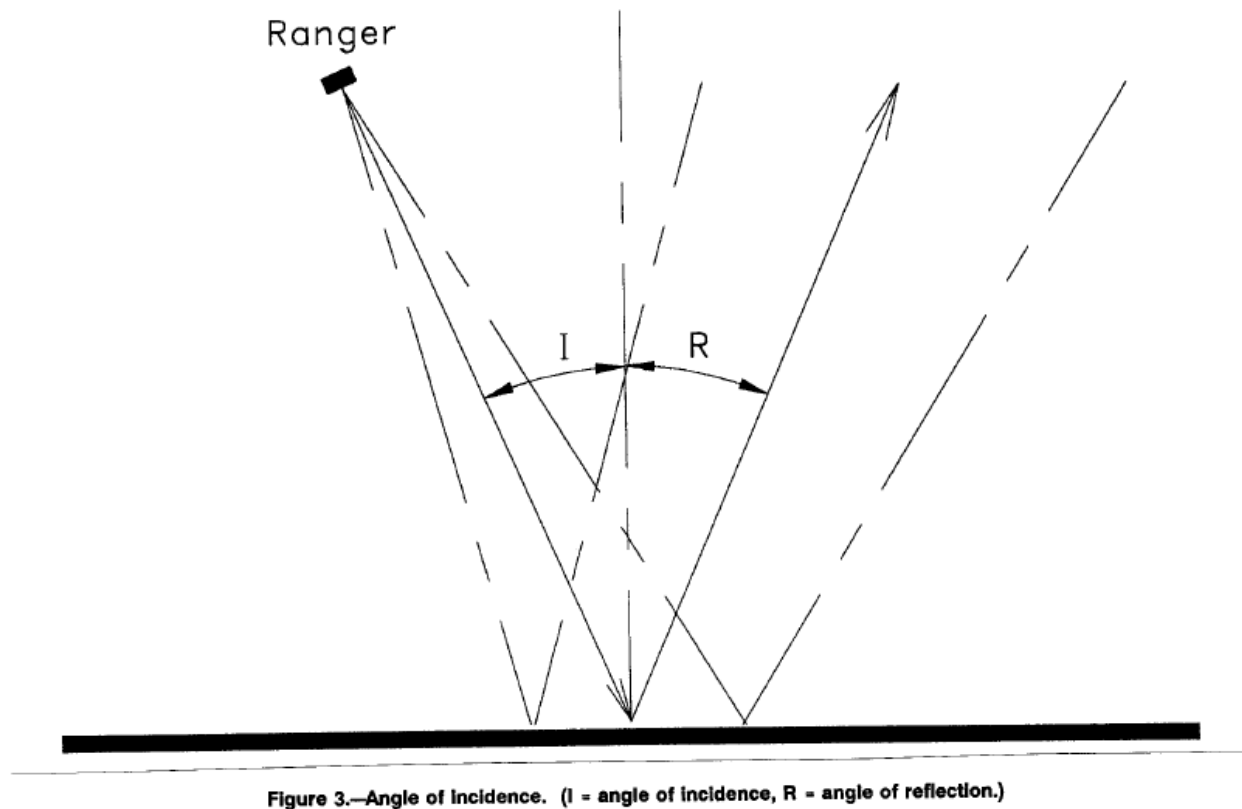
$$c = 331 + 0.6T \frac{\text{m}}{\text{s}}$$

where T is temperature in Celsius

- ▶ humidity affects c
- ▶ modern electronics can easily measure elapsed time with sufficient precision to obtain good distance resolution

Ultrasound Range Sensors

- ▶ most materials are specular reflectors of ultrasound



Ultrasound Range Sensors

- ▶ multiple reflections produce erroneous distance measurements

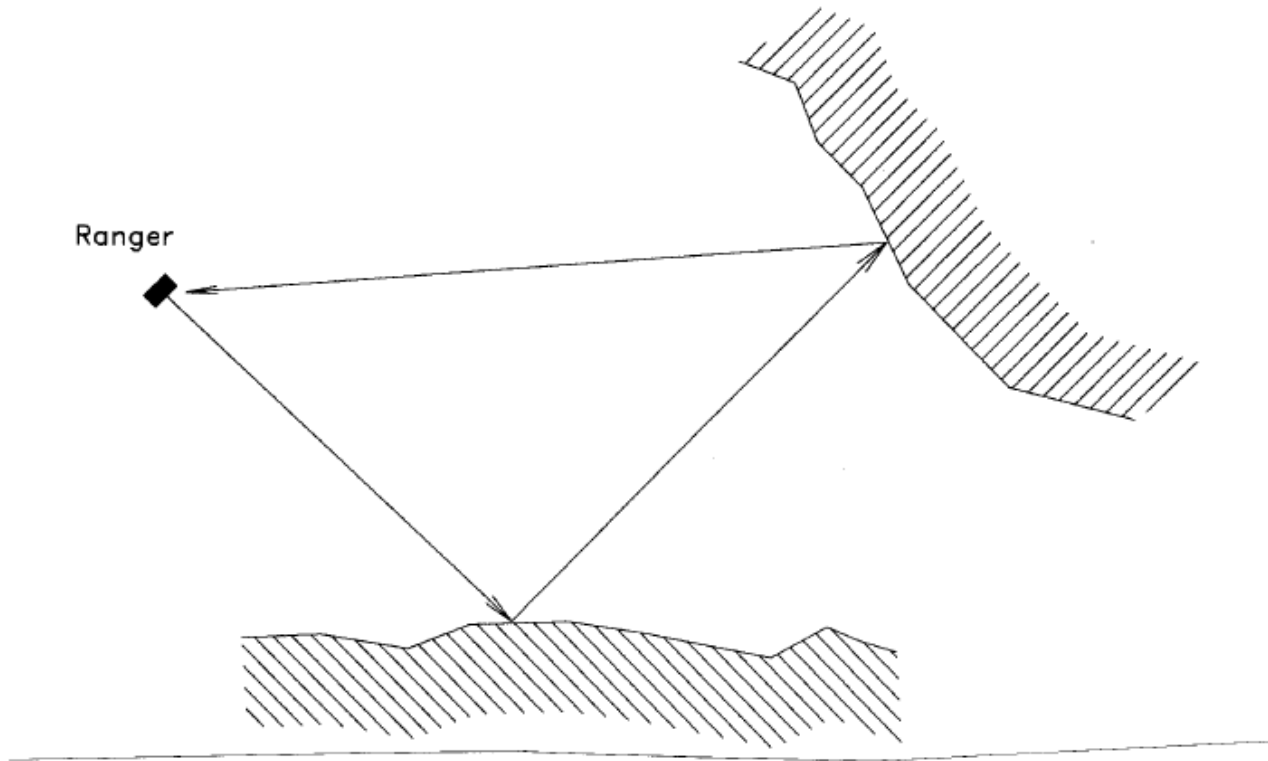


Figure 4.—Multiple reflections causing false range reading.

Ultrasound Range Sensors

- unfocussed ultrasound transducers have a wide beam pattern with significant side lobes

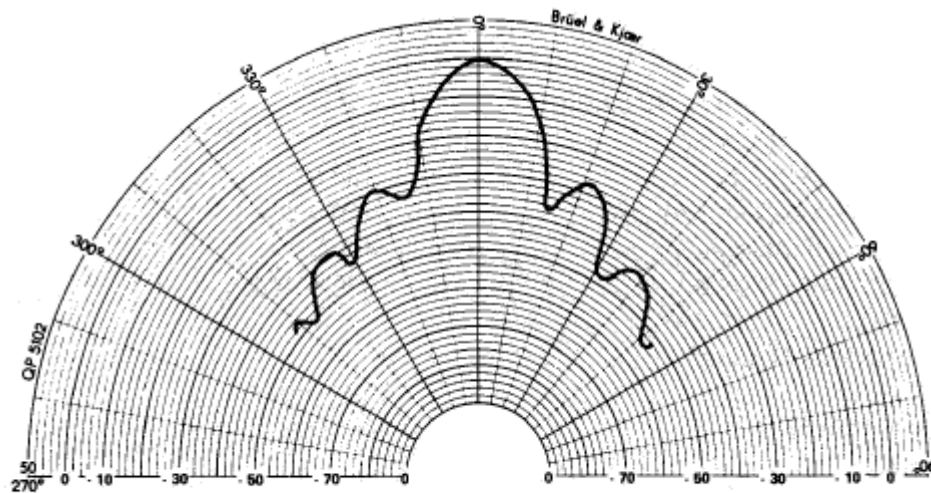


Figure 2: Typical propagation pattern for the Polaroid 6500 Series ultrasonic sensor. Courtesy of Polaroid [1].

Cao and Borenstein, “Experimental Characterization of Polaroid Ultrasonic Sensors in Single and Phased Array Configuration”

Ultrasound Range Sensors

- ▶ beamwidth + side lobes leads to spurious measurements

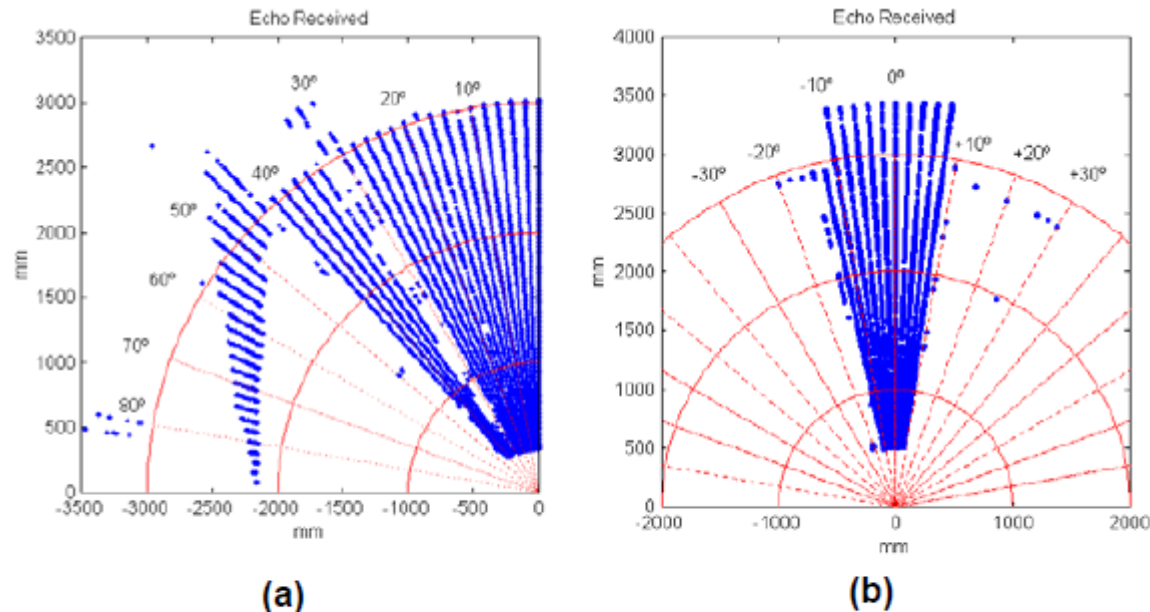


Figure 4: Baseline results for measuring distance to (a) the board and (b) the pole placed at different distances and with the sonar panned to different angles between 0 and 90°.

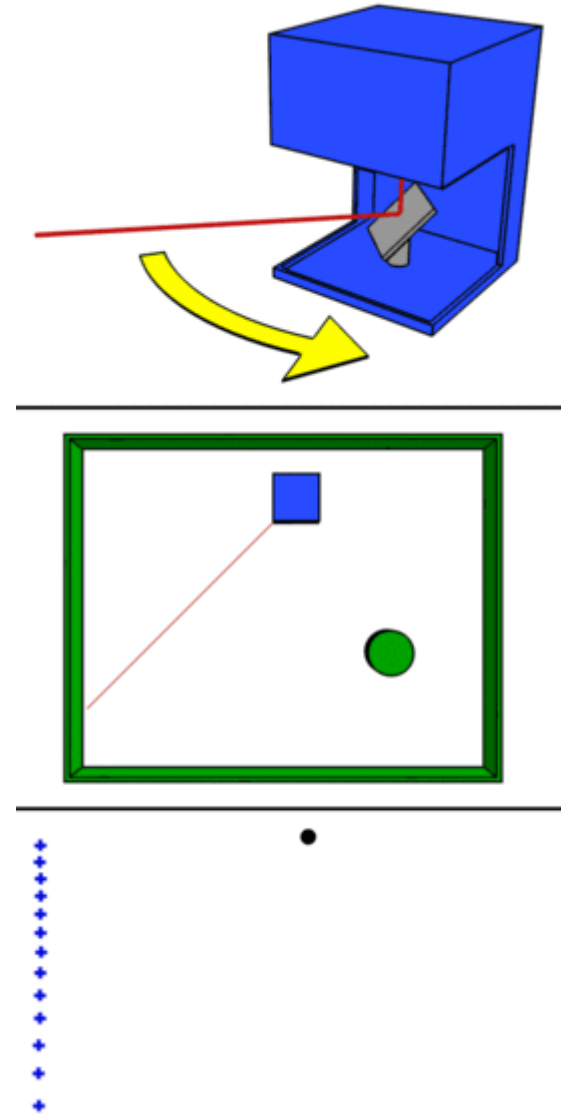
Cao and Borenstein, “Experimental Characterization of Polaroid Ultrasonic Sensors in Single and Phased Array Configuration”

Time of Flight Sensor

- ▶ <https://www.adafruit.com/product/3317>
- ▶ appear in laser tape measures
- ▶ array of time of flight sensors are use in time of flight cameras

LIDAR

- ▶ light detection and ranging
- ▶ commercial range finder
disassembled



LIDAR

- ▶ for time of flight sensor $d = \frac{1}{2} c \Delta t$

- ▶ speed of light $c = 3 \times 10^8 \frac{\text{m}}{\text{s}}$

1 ns = 150 mm

100 ps = 15 mm

10 ps = 1.5 mm

- ▶ typical angular resolution below 1 degree
- ▶ typical errors on the order of 10 cm or less
- ▶ cost > \$1,000

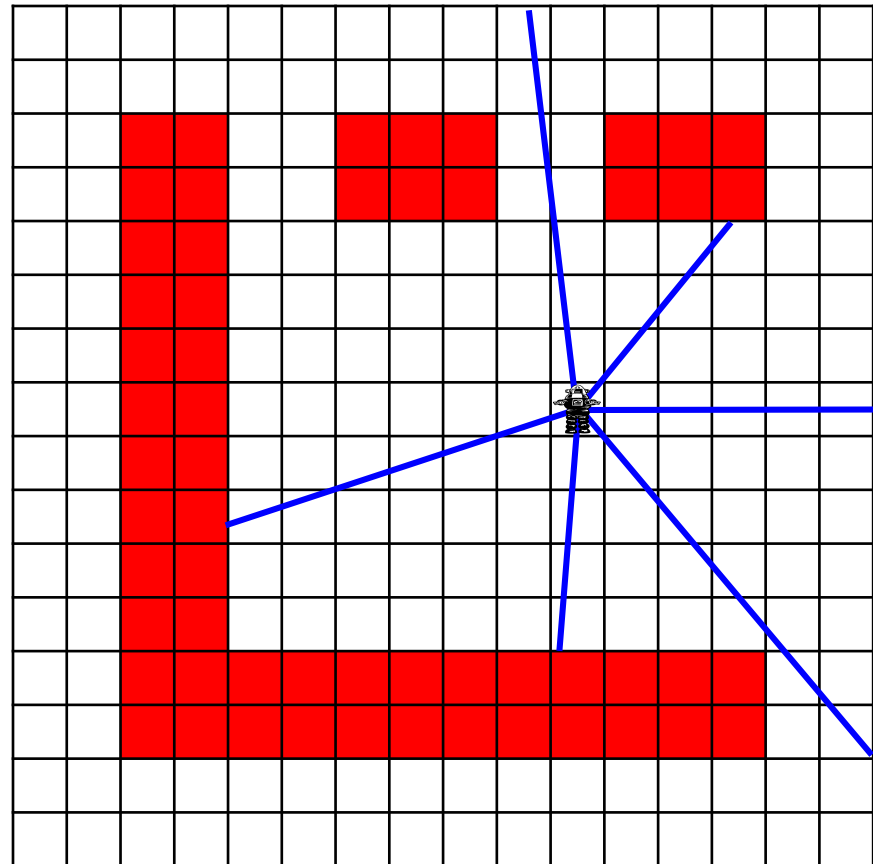
Beam Models of Range Finders

- ▶ given the map and the robot's location, find the probability density that the range finder detects an object at a distance z_t^k along a beam

$$p(z_t^k | x_t, m)$$

the k is here because range sensors typically return many measurements at one time; e.g., the sensor might return a full 360 degree scan made up of K measurements at once

$$z_t = \left\{ z_t^1, z_t^2, \dots, z_t^k, \dots, z_t^K \right\}$$



Beam Models of Range Finders

- ▶ most range finders have a minimum and maximum range
- ▶ we seek a model that can represent
 1. the correct range measurement with noise
 2. unexpected obstacles
 3. failures
 4. random measurements

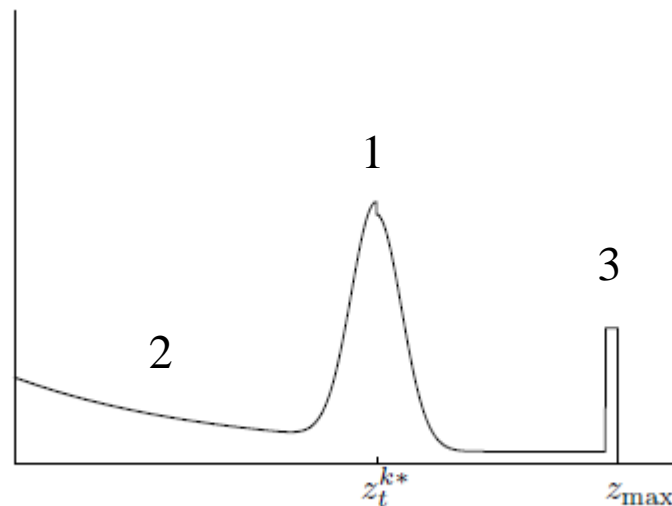


Figure 6.4 “Pseudo-density” of a typical mixture distribution $p(z_t^k | x_t, m)$.

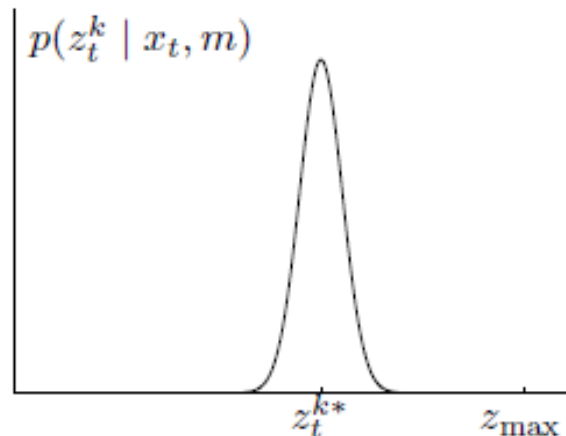
Beam Models of Range Finders

I. Correct Measurement with Noise

- ▶ suppose that the beam intersects an obstacle at a range of z_t^{k*}
 - ▶ model this measurement as a narrow Gaussian with mean z_t^{k*}

$$p_{\text{hit}}(z_t^k | x_t, m) = \begin{cases} \eta N(z_t^k; z_t^{k*}, \sigma_{\text{hit}}^2) & \text{if } 0 \leq z_t^k \leq z_{\text{max}} \\ 0 & \text{otherwise} \end{cases}$$

(a) Gaussian distribution p_{hit}



Beam Models of Range Finders

2. Unexpected Obstacles

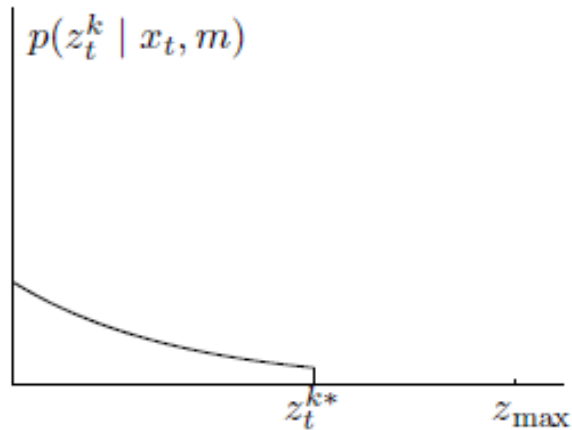
- ▶ in a dynamic environment there will be obstacles not found on a static map; these obstacles will cause range measurements shorter than expected
- ▶ if such obstacles appear continuously and independently at a constant average rate then they can be modeled as a Poisson process
- ▶ the time between events in a Poisson process has an exponential distribution with probability density function

$$f(x; \lambda) = \begin{cases} \lambda e^{-\lambda x}, & x \geq 0, \\ 0, & x < 0. \end{cases}$$

Beam Models of Range Finders

$$p_{\text{short}}(z_t^k | x_t, m) = \begin{cases} \eta \lambda_{\text{short}} e^{-\lambda_{\text{short}} z_t^k} & \text{if } 0 \leq z_t^k \leq z_t^{k*} \\ 0 & \text{otherwise} \end{cases}$$

(b) Exponential distribution p_{short}

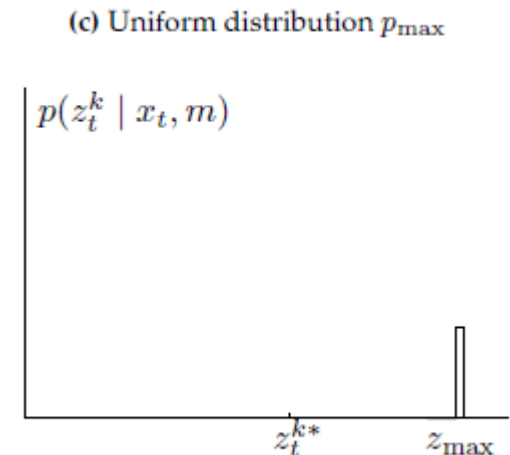


Beam Models of Range Finders

3. Failures

- ▶ range finders can fail to sense an obstacle in which case most sensors return z_{\max}
- ▶ modeled as a point mass distribution centered at z_{\max}

$$p_{\max}(z_t^k | x_t, m) = \begin{cases} 1 & \text{if } z_t^k = z_{\max} \\ 0 & \text{otherwise} \end{cases}$$

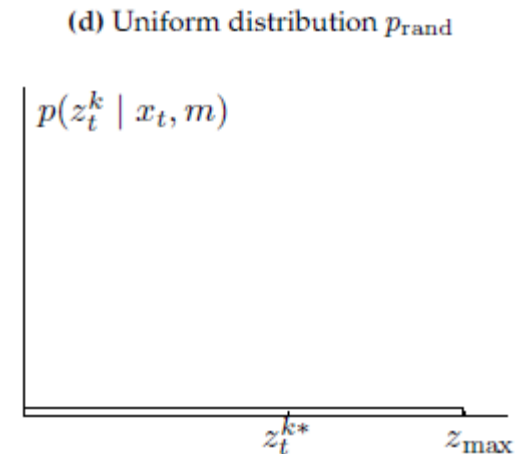


Beam Models of Range Finders

4. Random Measurements

- ▶ unexplainable measurements are modeled as a uniform distribution over the range $[0, z_{\max}]$

$$p_{\text{rand}}(z_t^k | x_t, m) = \begin{cases} \frac{1}{z_{\max}} & \text{if } 0 \leq z_t^k \leq z_{\max} \\ 0 & \text{otherwise} \end{cases}$$



Beam Models of Range Finders

- ▶ the complete model is a weighted sum of the previous four densities with weights

$$w_{\text{hit}} + w_{\text{short}} + w_{\text{max}} + w_{\text{rand}} = 1$$

$$p(z_t^k | x_t, m) = \begin{bmatrix} w_{\text{hit}} \\ w_{\text{short}} \\ w_{\text{max}} \\ w_{\text{rand}} \end{bmatrix}^T \begin{bmatrix} p_{\text{hit}}(z_t^k | x_t, m) \\ p_{\text{short}}(z_t^k | x_t, m) \\ p_{\text{max}}(z_t^k | x_t, m) \\ p_{\text{rand}}(z_t^k | x_t, m) \end{bmatrix}$$